

Name: _____ Date: _____

Answer Key: Dissect Cosmic Constants: A College Calculus-Based Measurement Quiz

Evaluate dimensional homogeneity and relativistic corrections across non-Euclidean frameworks where standard SI derivations face extreme astrophysical constraints.

1. When deriving the Planck length contextually, which synthesis of fundamental constants (G , \hbar , and c) maintains dimensional consistency for L ?

Answer: A) $\sqrt{G\hbar/c^3}$

Dimensional analysis shows that the square root of (gravitational constant * reduced Planck constant / speed of light cubed) yields the dimension of length ($\sim 1.6 \times 10^{-35}$ m).

2. Regarding the 2019 redefinition of SI base units, the value of the _____ is now fixed by defining the numerical value of the Boltzmann constant (k).

Answer: B) Kelvin

The Kelvin was redefined by fixing the Boltzmann constant to exactly 1.380649×10^{-23} J/K, linking thermal energy directly to temperature.

3. In a non-inertial reference frame, the measured 'proper time' between two events is a Lorentz invariant and remains unchanged regardless of the observer's velocity.

Answer: A) True

Proper time is the interval measured by a clock in the rest frame of the events; it is a scalar invariant in 4-dimensional Minkowski spacetime.

4. A Josephson Junction is primarily utilized in metrology to realize the SI volt by relating it to which two fundamental physical constants?

Answer: C) The Elementary charge and the Planck constant

The Josephson effect relates voltage to frequency via the Josephson constant ($K_J = 2e/h$), utilizing the elementary charge and Planck's constant.

5. When examining the systematic error in a high-precision interferometer, the 'Type B' evaluation of uncertainty is based on _____.

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Answer: C) Non-statistical scientific judgment and calibration data

Type B uncertainty evaluation uses available info (spec sheets, previous data) rather than the statistical analysis of current repeated measurements (Type A).

6. Calculate the radiant flux (Watts) of a blackbody source if its luminous intensity is 683 candelas at a frequency of 540×10^{12} Hz, assuming monochromatic emission.

Answer: B) 1 W

By definition, the candela is the luminous intensity of a source emitting monochromatic radiation of frequency 540×10^{12} Hz with a radiant intensity of 1/683 Watts per steradian.

7. The SI base unit for mass is no longer determined by a physical artifact (the 'Le Grand K') but is instead realized via the Kibble balance and Planck's constant.

Answer: A) True

Since 2019, the kilogram is defined by taking the fixed numerical value of the Planck constant (h) to be $6.62607015 \times 10^{-34} \text{ kg m}^2 \text{ s}^{-1}$.

8. In fluid dynamics, the Reynolds number is a dimensionless quantity. Which ratio of units correctly yields a dimensionless result for $Re = (\rho v d)/\mu$?

Answer: A) $(\text{kg}/\text{m}^3)(\text{m}/\text{s})(\text{m}) / (\text{kg}/(\text{m}\cdot\text{s}))$

Expanding the units: [Density: M/L^3] * [Velocity: L/T] * [Length: L] / [Dynamic Viscosity: $\text{M}/(\text{L}\cdot\text{T})$] results in all units canceling out ($\text{M}^0\text{L}^0\text{T}^0$).

9. For a Quantum Hall Effect experiment measuring Resistance (R_H), the Von Klitzing constant (R_k) equates the unit 'Ohm' to the ratio _____.

Answer: A) h / e^2

The Von Klitzing constant is defined as $R_k = h/e^2$, providing a highly stable and reproducible quantum standard for electrical resistance.

10. Even if a measurement is perfectly precise (zero variance), it can still possess high systematic error if the instrument is poorly calibrated.

Answer: A) True

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Precision refers to the repeatability of the data; a thermometer that consistently reads 50.00C for a 0.00C ice bath is perfectly precise but wildly inaccurate due to bias.